Introduction

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How would you define "machine learning"?

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- How is machine learning similar/different from computer programming?
 - Computer programs rely on written rules, machine learning develops rules by finding patterns in examples
- How is machine learning similar/different from statistics?
 - Statistics focuses on inference about a population using a sample, machine learning seeks generalizable predictive patterns



Image credit: BBN Times

Example

Consider two predictors, x_1 and x_2 , and an outcome y of "healthy" or "unhealthy". Can these predictors be used to accurately *classify* an observation?



x1

Example (cont.)

Yes! In this example, the true relationship between predictors and the outcome is given by the blue ellipse



x1

Learning?

As a human, you might observe that the healthy data-points tend to fall between 2 and 8 in x_1 and x_2 , so you might propose the following *classification model*:



This simple model correctly classifies 178 of 200 data-points.

Reducible vs. Irreducible Error

Let's revisit the true relationship between x_1 , x_2 , and y. Notice that some "healthy" data-points are outside the ellipse, and some "unhealthy" ones are inside it:



- The misclassification of these examples is known as the irreducible error (sometimes called "Bayes error")
 - Even the *best possible model* still cannot perfectly predict every outcome

Irreducible Error in Real Life

Is a digit a "5" or something else?



How might the concept of irreducible error manifest in this application?

Irreducible Error in Real Life

We could know the exact "rules" used to make a "5", but it's possible we encounter examples of "5" that look more like a "6".



Even state of the art classifiers (which approach the irreducible error rate) misclassify $\sim 0.5\%$ of handwritten digits (source)

Irreducible error will always exist, the important question is "how much?" Consider the following scenarios:

- Classifying examples of "5" handwritten by a doctor
- Classifying examples of "5" created by a laser printer

While the precise amount of irreducible error in a machine learning problem is generally unknown, we often have a sense of what it might be.

Reducible Error

The primary goal of machine learning is to *learn rules* that minimize *reducible error*. Consider the following classifier:



Has this classifier reduced the error rate to zero?

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- We generally aren't interested in the error rate for the observed examples
 - Instead, we'd like to minimize reducible error on new examples that our model hasn't yet seen
- Standard procedure is to divide the available data into training and testing sets
 - The training set is used to learn a collection of rules
 - The testing set is used to evaluate how well these rules perform on data that hasn't been seen by the learner

Training, Testing, and Error

Consider a hypothetical example with an irreducible error of "20 units":



Training error can always be reduced by increasing the model complexity (ie: learning more rules), but testing error will never drop below the irreducible error (probabilistically speaking, it might for a single test set) Reducible error can arise in one of two ways: bias or variance

- Bias is when a learner lacks the structural flexibility to detect aspects of the true relationship between the predictors and the outcome
- Variance is when a learner is overly sensitive to chance artifacts present in the data (ie: the manifestations of irreducible error)

Poor performance due to high bias is called *underfitting*, while poor performance due to high variance is called *overfitting*

How would you compare the bias and variance of the following learners (a rectangle vs. an n-dimensional polygon)?



- So far we've focused on classifying a binary categorical outcome, a scenario where *classification accuracy* provides a natural framework for understanding a method's error
 - We'll talk about more sophisticated ways to evaluate error for categorical outcomes next week
- What if our goal is to predict a numeric outcome?

For a numeric outcome, it's most natural to measure error by summarizing the distances between predicted and observed outcomes:

Root Mean Squared Error: RMSE = \sqrt{\frac{1}{n}\sum_{i=1}^n(y_i - \hfrac{y}_i)^2}\$
Mean Absolute Error: MAE = \frac{1}{n}\sum_{i=1}^n|y_i - \hfrac{y}_i|\$

In each definition, y_i is the observed outcome for the i^{th} example (data-point) and \hat{y}_i is the predicted outcome for that example.

- Machine learning applications involving a *numeric outcome* are called regression tasks
 - Applications involving a categorical outcome are called classification tasks
- We define error differently for each type of task
 - The bias-variance trade-off and irreducible error still apply to both scenarios

Machine Learning without an Outcome?

For most of this semester, we'll focus on machine learning tasks involving a pre-selected or derived outcome
These are known as supervised learning tasks
Other learning tasks, such as clustering or dimension reduction, can be achieved without designating an outcome
These are known as unsupervised learning tasks

Overview



- 1. Definitions and examples of reducible vs. irreducible error
- 2. The bias-variance trade-off
- 3. The reason for creating a training and testing split
- 4. Definitions and differences between classification and regression