# Sampling from a Population 

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## Outline

1. Samples and populations

- Definitions, examples, and notation

2. Sources of sampling error

- Sampling bias and variability

3. Sampling methods

- Convenience sampling, simple random sampling, and other approaches


## Introduction

Suppose a biologist wants to learn about the species of fish that reside within a particular lake

1) Do they need to capture and study every fish in this lake in order to achieve their goal?
2) What trade-offs are involved in collecting data on only some of the fish rather than all of them?

## Sampling from a population

The data we collect is typically a sample, or a subset of cases, from a broader population, the collection of all cases we might be interested in:


## Population



Inference

Note: We'll denote the number of cases in our sample as $n$ and the size of the population as $N$ (which is sometimes unknown)

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## Sampling from a population

- Inference addresses the statistical question: "how reliably will trends in a sample reflect what is true of the population?"
- For example, if two variables, $X$ and $Y$, have a correlation of $r=0.71$ in a sample, how do you think these variables are related in the population?
- As a starting point, we might use the sample correlation as an estimate of the population-level correlation
- If the sample data are representative, this estimate should be close to the population-level correlation


## Notation for estimates and population parameters

Statisticians use notation to distinguish population parameters (things we want to know) from estimates (things derived from a sample):

|  | Population Parameter | Estimate (from sample) |
| :--- | :---: | :---: |
| Mean | $\mu$ | $\bar{x}$ |
| Standard Deviation | $\sigma$ | $s$ |
| Proportion | $p$ | $\hat{p}$ |
| Correlation | $\rho$ | $r$ |
| Regression | $\beta_{0}, \beta_{1}$ | $b_{0}, b_{1}$ |

## Two sources of sampling error

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2) Sampling Variability - since a sample doesn't include all of the population, any individual sample might differ from the population due to random chance (ie: "the luck of the draw")

## Sampling error

Four different sampling procedures:


Each "dot" represent an estimate from a different sample

## Remarks on sampling error

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- Sampling procedures with high variance might seem problematic, but statisticians have developed tools (rooted in probability theory) to facilitate decision making in the face of this uncertainty


## Practice

- In 1936, Franklin Roosevelt was up for re-election versus Republican candidate Alfred Landon
- Prior to the election, the Literary Digest sampled 2.4 million voters and predicted a landslide victory for Landon: $57 \%$ to 43\%
- The Literary Digest had correctly predicted every election since 1916


## Practice

- In 1936, Franklin Roosevelt was up for re-election versus Republican candidate Alfred Landon
- Prior to the election, the Literary Digest sampled 2.4 million voters and predicted a landslide victory for Landon: $57 \%$ to 43\%
- The Literary Digest had correctly predicted every election since 1916
- However, Roosevelt won the actual election by a landslide: $62 \%$ to $38 \%$

1) What is the population and what is the sample
2) What is the population parameter and what is the sample estimate?
3) Was the Digest's inaccurate estimate likely due to sampling bias or sampling variability (or both)?

## Practice (solution)

1) The population is all of the people who voted in the 1936 election. The sample is the 2.4 million voters contacted by the Literary Digest.
2) The population parameter is the proportion who voted for Roosevelt (or Landon since either proportion would tell you the other). The sample estimate would then be $43 \%$ (the proportion of those sampled by the Digest who said they'd vote for Roosevelt)
3) Sampling bias - the sample size was enormous (making variability a non-issue). The sample was biased towards wealthy in

## Types of bias in the Literary Digest example

## Selection Bias

- The Literary Digest sent 10 million questionnaires to addresses gathered from telephone books and club memberships
- This disproportionately screened out the poor; Only 1 in 4 households owned a telephone at the time, and club members tended to be upper class
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## Non-response Bias

- Of the 10 million questionnaires, only 2.4 million were returned
- Respondents tend to be different from non-respondents
- The 2.4 million respondents likely weren't even representative of the 10 million people polled


## Other sources of bias

2. Non-ignorable Missing Data - Subjects who are excluded from analysis due to missing data differ in important ways from those with complete data
3. Social Desirability Bias - Respondents tend to answer questions in ways that portray themselves in a positive light Link
4. Interviewer Bias - The interviewer causes subjects to the behave differently than they otherwise would

## Common sampling methods

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- Cons: can be difficult to execute
- Stratified or cluster random sampling - randomly select cases separately from different population segments, potentially using different strategies for each segment
- Pros: low potential for sampling bias, more flexibility than simple random sampling
- Cons: data analysis becomes complicated (sampling weights, etc.)


## Practice

With your group, discuss whether each of the following describe a sample or a population. If the data are a sample, describe the target population and whether the sample is biased or representative.

1. To estimate the size of trout in a lake, an angler records the weight of the 12 trout he catches over a weekend
2. The Department of Transportation announces that of the 250 million registered cars in the US, $2.1 \%$ are hybrids
3. An online poll seeking to learn about adult workers asks: "What do you think of having an everyday uniform for work, like what Steve Jobs did?" $24 \%$ of people said they loved the idea

## Practice (solution)

1. This is a sample, the population is all trout in the lake. It is a biased sample because the angler isn't randomly catching fish, he is likely fishing in a single spot and is more likely to catch certain sizes of trout
2. This is a population, the DOT has information on all registered cars in the US.
3. This is a sample, the population is all adult workers. It is a biased sample due being an online poll, and the social desirability typically associated with Steve Jobs.

## Conclusion

1. Samples and populations

- a sample is a subset of cases from a population that is used to make inferences

2. Sources of sampling error

- Sampling bias is the result of a sampling procedure that systematically over (or under) selects certain types of cases
- Sampling variability decreases for larger samples

3. Sampling methods

- Convenience sampling is easy, but can be biased (though not necessarily)
- Simple random sampling is unbiased, but can be difficult to implement

